CONGRUENT TRIANGLES

Congruent Triangle



Let there be two triangles ABC and DEF. Out of the total six (1-1) correspondences that can be established between Δ ABC and Δ DEF. One of the choices is explained below.

In the correspondence \triangle ABC \leftrightarrow \triangle DEF it means.

 $\angle A \leftrightarrow \angle D$ ($\angle A$ corresponds to $\angle D$)

 $\angle B \leftrightarrow \angle E$ ($\angle B$ corresponds to $\angle E$)

 $\angle C \leftrightarrow \angle F$ ($\angle C$ corresponds to $\angle F$)

 $\overline{AB} \leftrightarrow \overline{DE}$ (\overline{AB} corresponds to \overline{DE})

 $\overline{BC} \leftrightarrow \overline{EF}$ (\overline{BC} corresponds to \overline{EF})

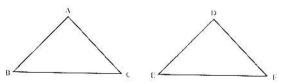
 $\overline{CA} \leftrightarrow \overline{FD}$ (\overline{CA} corresponds to \overline{FD})

Congruency of Triangles

Two triangles are said to be congruent written symbolically as, \cong , if there exists a correspondence between them such that all the corresponding sides and angles are congruent i.e.

$$If \begin{cases} \overline{AB} \cong \overline{DE} \\ \overline{BC} \cong \overline{EF} \\ \overline{CA} \cong \overline{FD} \end{cases} \quad \text{and} \quad \begin{cases} \angle A \cong \angle D \\ \angle B \cong \angle E \\ \angle C \cong \angle F \end{cases}$$

Then ∆ABC≅∆DEF



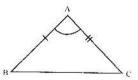
Note

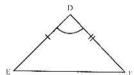
- (i) These triangles are congruent w.r.t. the above mentioned choice of the (1-1) correspondence.
- (ii) ΔABC≅ΔABC
- (iii) ΔABC≅ΔDEF ⇔ ΔDEF≅ΔABC
- (iv) If $\triangle ABC \cong \triangle DEF$ and $\triangle ABC \cong \triangle PQR$, then $\triangle DEF \cong \triangle PQR$

In any correspondence of two triangles, if two sides and their included angle of one triangle are congruent to the corresponding two sides and their included angle of the other, then the triangles are congruent.

In \triangle ABC \leftrightarrow \triangle DEF, shown in the following figure.

$$If \begin{cases} \overline{AB} \cong \overline{DE} \\ \underline{\angle A} \cong \underline{\angle D} \\ \overline{AC} \cong \overline{DF} \end{cases}$$

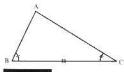


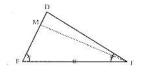


Then ∆ABC≅ADEF (S.A.S. Postulate)

Theorem

In any correspondence of two triangles, if one side and any two angles of one triangle are congruent to the corresponding, side and angles of the other, then the triangles are congruent. $(A.S.A \cong A.S.A)$





Given

In $\triangle ABC \leftrightarrow \triangle DEF$ $\angle B \cong \angle E$ $\overline{BC} \cong \overline{EF}$

$\angle C \cong \angle F$

To prove

 $\triangle ABC \leftrightarrow \triangle DEF$

Construction

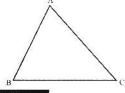
Suppose $\overline{AB} \not\equiv \overline{DE}$, take a point M on \overline{DE} such that $\overline{AB} \cong \overline{ME}$. Join M to F

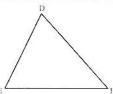
Proof

	Statements	Reasons
In	$\triangle ABC \leftrightarrow \triangle MEF$	
	$\overline{AB} \cong \overline{ME}$ (i)	Construction
	$\overline{BC} \cong \overline{EF}$ (ii)	Given
	∠B ≅ ∠E(iii)	Given
••	$\triangle ABC \cong \triangle MEF$	S.A.S. postulate
So,	∠C≅∠MFE	(Corresponding angles of congruent
		triangles)
But	∠C≅ ∠DFE	Given
	∠DFE ≅ ∠MFE	Both congruent to ∠C
This i	s possible only if D and M are the	
same j	points, and $\overline{\text{ME}} \cong \overline{\text{DE}}$	a a
So,	$\overline{AB} \cong \overline{DE}$ (iv)	$\overline{AB} \cong \overline{ME}$ (construction) and
Thus f	from (i), (iii) and (iv), we have	$\overline{\text{ME}} \cong \overline{\text{DE}} \text{ (proved)}$
	$\triangle ABC \cong \triangle DEF$	S.A.S. postulate

Example

In any correspondence of two triangles, if one side and any two angles of one triangle are congruent to the correspondence side and angles of the other, then the triangles are congruent. $(S.A.A \cong S.A.A.)$





Given

 $\frac{\text{In } \Delta ABC \leftrightarrow \Delta DEF}{BC \cong EF} , \ \angle A \cong \angle D , \ \ \angle B \cong \angle E$

To Prove

 $\triangle ABC \cong \triangle DEF$

	Statements	Reasons
In	$\triangle ABC \leftrightarrow \triangle DEF$	
	∠B ≅ ∠E	Given
	$\overline{BC} \cong \overline{EF}$	Given
	$\angle C \cong \angle F$ $\triangle ABC \cong \triangle DEF$	$\angle A \cong \angle D$, $\angle B \cong \angle E$, (Given) A.S.A. \cong A.S.A

Example

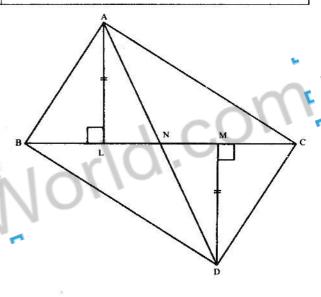
If $\triangle ABC$ and $\triangle DCB$ are on the opposite sides of common base \overline{BC} such that $\overline{AL} \perp \overline{BC}$, $\overline{DM} \perp \overline{BC}$, $\overline{AL} \cong \overline{DM}$, then \overline{BC} bisects \overline{AD} .

Given

 ΔABC and ΔDCB are on the opposite sides of \overline{BC} such that $\overline{AL} \perp \overline{BC}$, $\overline{DM} \perp \overline{BC}$, $\overline{AL} \cong \overline{DM}$ and \overline{AD} is cut by \overline{BC} at N.



 $\overline{AN} \cong \overline{DN}$



	Statements	Reasons	
In	$\Delta ALN \leftrightarrow \Delta DMN$ $\overline{AL} \cong \overline{DM}$ $\angle ALN \cong \angle DMN$ $\angle ANL \cong \angle DNM$ $\Delta ALN \cong \Delta DMN$	Given Each angle is right angle Vertical angles S.A.A. \cong S.A.A Corresponding sides of \cong Δ s.	
Heno	ce AN ≅DN	Corresponding sides of = 23.	

Exercise 10.1

1. In the given figure.

$$\overline{AB} \cong \overline{CB}, \angle 1 \cong \angle 2.$$

Prove that

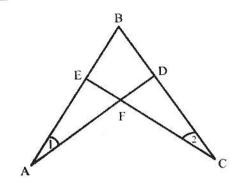
ΔABD ≅ΔCBE

Given

 $\overline{AB} \cong \overline{CB}$

 $\angle 1 = \angle 2$

To Prove



ΔABD ≅ ΔCBE Statements	Reasons
In $\triangle ABD \leftrightarrow \triangle CBE$ $\overline{AB} \cong \overline{CB}$ $\angle 1 \cong \angle 2$ $\angle ABD \cong \angle CBE$ $\therefore \triangle ABD \cong \triangle CBE$	Given Given Common angle A.S.A ≅ A.S.A

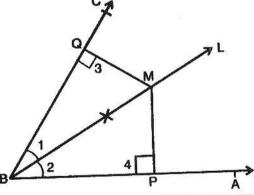
(2) From a point on the bisector of an angle, perpendiculars are drawn to the arms of the angle. Prove that these perpendiculars are equal in measure.

Given

 $\angle ABC$, \overline{BL} he bisector of $\angle ABC$, M any point on \overline{BL} , \overline{MP} perpendicular on \overline{AB} , $\overline{MQ} | | \overline{BC}$.

To Prove

 $\overline{\text{MP}} \cong \overline{\text{MQ}}$



Statements	Reasons
In $\triangle BMP \leftrightarrow \triangle BMQ$ $\angle 1 \cong \angle 2$ $\angle 3 \cong \angle 4$ $\overline{BM} \cong \overline{BM}$ $\triangle BMP \cong \Delta BMQ$ $\overline{PM} \cong \overline{QM}$	BL bisects ∠PBQ Each = 90° Common A.S.A≅ A.S.A Corresponding sides of the congruent triangles.

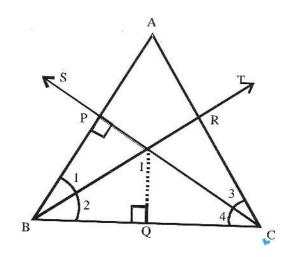
In a triangle ABC, the bisectors (3) of ∠B and ∠C meet in a point I. Prove that I is equidistant from the three sides of AABC.

Given

In $\triangle ABC$, \overrightarrow{BT} , \overrightarrow{CS} are the bisectors of the angles B and C respectively.

To Prove

I is equidistant from the three sides of $\triangle ABC$ i.e. $\overline{IP} \cong \overline{IQ} \cong \overline{IR}$



Construction

 $\overline{IR} \bot \overline{AC}, \overline{IQ} \bot \overline{BC}, \overline{IP} \bot \overline{AB}$

	Statements	Reasons
In	$\Delta IPB \leftrightarrow \Delta IQB$	1-4/01
	∠1 ≅ ∠2	Given
	$\angle P \cong \angle Q$	Each = 90°
	IB ≅ IB	Common
	$\Delta IPB \cong \Delta IQB$	$A.S.A \cong A.S.A$
	$\overline{IP} \cong \overline{IQ} \dots (i)$	Corresponding sides of congruent triangles
Simila	arly Δ IRC \cong Δ IQC	1
	$\overline{IQ} \cong \overline{IR} \dots (ii)$	Corresponding sides of congruent triangles
	$\overline{\text{IP}} \cong \overline{\text{IQ}} \cong \overline{\text{IR}}$	By (i) and (ii)

Theorem

If two angles of a triangle are congruent, then the sides opposite to them are also congruent.

Given

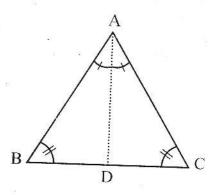
In $\triangle ABC$, $\angle B \cong \angle C$

To Prove

 $\overrightarrow{AB} \cong \overrightarrow{AC}$

Construction

)raw the bisector of $\angle A$, meeting \overline{BC} at the point D.



	Statements	Reasons
In	$\triangle ABD \leftrightarrow \triangle ACD$	
	$\overline{\mathrm{AD}}\cong\overline{\mathrm{AD}}$	Common
	$\angle B \cong \angle C$	Given
	∠BAD ≅ ∠CAD	Construction
.:.	$\Delta ABD \cong \Delta ACD$	$S.A.A. \cong S.A.A.$
Hend	ce $\overline{AB} \cong \overline{AC}$	Corresponding sides of congruent triangles

Example

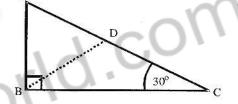
If one angle of a right triangle is of 30°, the hypotenuse is twice as long as the side opposite to the angle.

Given

In $\triangle ABC$, $m\angle B = 90^{\circ}$ and $m\angle C = 30^{\circ}$

To Prove

$$m\overline{AC} = 2m\overline{AB}$$



Construction

At B, construct $\angle CBD$ of 30° . Let \overline{BD} cut \overline{AC} at the point D.

Proof

Statements	Reasons
In $\triangle ABD$, $m\angle A = 60^{\circ}$	$m\angle ABC = 90^{\circ}, m\angle C = 30^{\circ}$
$m\angle ABD = m\angle ABC - m\angle CBD = 60^{\circ}$	
V	$m\angle ABC = 90^{\circ}, m\angle CBD = 30^{\circ}$
$\therefore \qquad \text{m}\angle \text{ADB} = 60^{\circ}$	Sum of measures of ∠s of a∆ is 180°
\therefore \triangle ABD is equilateral	Each of its angles is equal to 60°
$\therefore \qquad \overline{AB} \cong \overline{BD} \cong \overline{AD}$	Sides of equilateral Δ
$In\Delta BCD, \overline{BD} \cong \overline{CD}$	$\angle C = \angle CBD$ (each of 30°).
Thus	
$\overline{MAC} = \overline{MAD} + \overline{MCD}$	$\overline{AD} \cong \overline{AB}$ and $\overline{CD} \cong \overline{BD} \cong \overline{AB}$
$= m\overline{AB} + m\overline{AB}$	
=2(mAB)	

Example

If the bisector of an angle of a triangle bisects the side opposite to it, the triangle is isosceles.

Given

In $\triangle ABC$, \overrightarrow{AD} bisects $\angle A$ and $\overrightarrow{BD} \cong \overrightarrow{CD}$

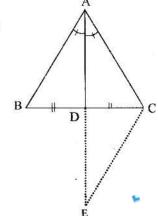
To Prove

 $\overline{AB} \cong \overline{AC}$

Construction

Produce \overline{AD} to E, and take $\overline{ED} \cong \overline{AD}$.

joint C to E



Proof

Statements		Reasons
In	$\triangle ABD \leftrightarrow \triangle EDC$	14 60
	AD≅ED	Construction
	∠ADB ≅ ∠EDC	Vertical angles
	BD≅CD	Given
	$\triangle ADB \cong \triangle EDC$	S.A.S. Postulate
<i>:</i> .	<u>AB</u> ≅ <u>EC</u> (1)	Corresponding sides of $\cong \Delta s$
and	∠BAD ≅ ∠E	Corresponding angles of $\cong \Delta s$
But	∠BAD ≅ ∠CAD	Given
:.	∠E≅∠CAD	Each ≅ ∠BAD
In	$\triangle ACE, \overline{AC} \cong \overline{EC} \dots (2)$	\angle E \cong \angle CAD (proved)
Henc	e AB ≅ AC	From (1) and (2)

Exercise 10.2

Prove that a point, which is equidistant from the end points of a line segment, is on the right bisector of the line segment.

Given

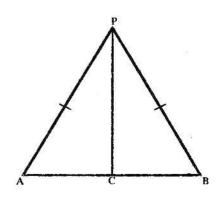
 \overline{AB} is a line segment. Point P is such that $\overline{PA} \cong \overline{PB}$

To Prove

Point P is on the right bisector of \overline{AB} .

Construction

Join P to C, the midpoint of AB



Proof Statements	Reasons
In $\triangle ACP \leftrightarrow \triangle BCP$ $\overline{PA} \cong \overline{PB}$ $\overline{PC} \cong \overline{PC}$ $\overline{AC} \cong \overline{BC}$ $\triangle ACP \cong \triangle BCP$ $\angle ACP \cong \angle BCP$ (i) $\triangle But \ m \angle ACP + m \angle BCP = 180^{\circ}$ (ii) $\triangle ACP = m \angle BCP = 90^{\circ}$ or $\overline{PC} \perp \overline{AB}$ (iii) $\overline{Also} \ \overline{CA} \cong \overline{CB}$ (iv) $\overline{PC} \ is a \ right \ bisector$ Of \overline{AB} i.e, the point P is on the right bisector of \overline{AB} .	Given Common Construction S.S.S ≅ S.S.S Corresponding angles of congruent triangles supplementary angles, From (i) and (ii) m∠ACP = 90° (proved) construction from (iii) and (vi)

Theorem

In a correspondence of two triangles, if three sides of one triangle are congruent to the corresponding three sides of the other, then the two triangles are congruent.

$$(S.S.S. \cong S.S.S.)$$

Given

In $\triangle ABC \leftrightarrow \triangle DEF$

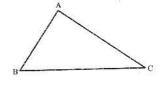
 $\overline{AB} \cong \overline{DE}, \overline{BC} \cong \overline{EF}$ and $\overline{CA} \cong \overline{FD}$

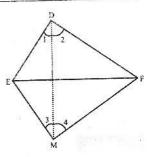
To Prove

 $\triangle ABC \cong \triangle DEF$

Construction

Suppose that in ΔDEF the side \overline{EF} is not smaller than any of the remaining two sides. On \overline{EF} construct a ΔMEF in which, \angle $FEM \cong \angle B$ and $\overline{ME} \cong \overline{AB}$. Join D and M. As shown in the above figures we label some of the angles as 1,2,3 and 4.





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	Statements	Reasons
In	ΔABC ↔ ΔMEF	
	BC≡EF	Given
	∠B ≅ ∠FEM	Construction
	AB≅ME	Construction
	$\triangle ABC \cong \triangle MEF$	S.A.S postulate
and	CA≅FM(i)	(Corresponding sides of congruent triangles)
Also	CA≅FD(ii)	Given
	FM≅FD	From (i) and (ii)
In	ΔFDM	100
	∠2 ≅ ∠4(iii)	FM≅FD (proved)
Simila	$arly \angle 1 \cong \angle 3 \dots (iv)$	17,00.
••	$m\angle 2 + m\angle 1 = m\angle 4 + m\angle 3$	{from (iii) and (iv)}
.: .	m∠EDF = m∠EMF	
Now,	In∆DEF ↔ AMEF	
	FD≅FM	Proved
And	m∠EDF ≅ m∠EMF	Proved
_ v	DE≅ME	Each one $\cong \overline{AB}$
	ΔDEF ≅ ΔMEF	S.A.S postulate
Also	ΔABC ≅ ΔMEF	Proved
Hence	ΔABC ≅ ΔDEF	Each $\Delta \cong \Delta MEF$ (Proved)

Example

If two isosceles triangles are formed on the same side of their common base, the line through their vertices would be the right bisector of their common base.

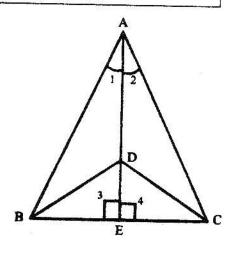
Given

 ΔABC and ΔDBC are formed on the same side of \overline{BC} such that

 $\overline{AB} \cong \overline{AC}, \overline{DB} \cong \overline{DC}, \overline{AD}$ meets \overline{BC} at E.

Laprove

BE≅CE, AE ⊥BC



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	Statements	Reasons
In	$\triangle ADB \leftrightarrow \triangle ADC$	
	$\overline{AB} \cong \overline{AC}$	Given
	$\overline{DB} \cong \overline{DC}$	Given
	$\overline{AD} \cong \overline{AD}$	Common
<i>:</i> .	$\triangle ADB \cong \triangle ADC$	S.S.S ≅ S.S.S.
••	∠1 ≅ ∠2	Corresponding angles of $\cong \Delta s$
In	$\triangle ABE \leftrightarrow \triangle ACE$	
	$\overline{AB} \cong \overline{AC}$	Given
	∠1 ≅ ∠2	Proved
	AE≅AE	Common
	$\triangle ABE \cong \triangle ACE$	S.A.S. postulate
•	BE≅CE	Corresponding sides of $\cong \Delta s$
	∠3 ≅ ∠4I	Corresponding angles of $\cong \Delta s$
	$m \angle 3 + m \angle 4 = 180^{\circ}$ II	Supplementary angles Postulate
	m∠3 = m∠4 = 90°	From I and II
Henc	e AE ⊥ BC	

Corollary: An equilateral triangle is an equiangular triangle.

Exercise 10.3

Q1. In the figure, $\overline{AB} \cong \overline{DC}$, $\overline{AD} \cong \overline{BC}$.

Prove that $\angle A \cong \angle C$, $\angle ABC \cong \angle ADC$.

Given

 $\overline{AB} \cong \overline{DC}$

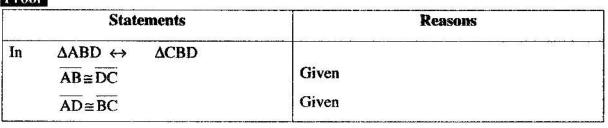
 $\overline{AD} \cong \overline{BC}$

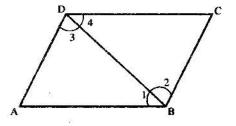
To prove

 $\angle A \cong \angle C$

∠ABC ≅ ∠ADC

Proof





	BD≅BD
	$\Delta ABD \cong \Delta CBD$
	$\angle A \cong \angle C$
	$\angle 1 \cong \angle 4 \dots (i)$
	$\angle 2 \cong \angle 3 \dots (ii)$
	$\angle 1 + \angle 2 = \angle 3 + \angle 4$
	∠ABC≅∠ADC
i i i i i i i i i i i i i i i i i i i	

Common

 $S.S.S \cong S.S.S$

Corresponding angles of congruent triangles Corresponding angles of congruent triangles Adding (i) and (ii)

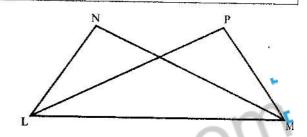
2. In the figure, $\overline{LN} \cong \overline{MP}$, $\overline{MN} \cong \overline{LP}$.

Prove that $\angle N \cong \angle P$, $\angle NML \cong \angle PLM$.

Given

LN≅MP

<u>LP</u>≅<u>MN</u>



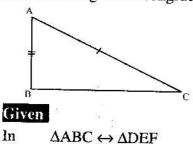
To prove

 $/N \simeq /P$

	Statements	Reasons
ln	Δ LMN \leftrightarrow Δ LMP	
	$\frac{LM \cong MP}{LP \cong \overline{MN}}$	Given Given
	<u>LM</u> ≅LM	Common
	Δ LMN \cong Δ LPM \angle N = \angle P \angle NML \cong \angle PLM	$S.S.S \cong S.S.S$ Corresponding angles of congruent triangles
,,,,,,		Corresponding angles of congruent triangles

Theorem

If in the correspondence of the two right-angled triangles, the hypotenuse and one side of one triangle are congruent to the hypotenuse and the corresponding side of the other, then the triangles are congruent. (H.S \cong H.S)



 $\angle B \cong \angle E$ (right angles)

CA≅FD, AB≅DE

, m. s	Statements	Reasons
In Now ∴ In	$m\angle DEF + m\angle DEM = 180^{\circ}(i)$ $m\angle DEF = 90^{\circ}(ii)$ $m\angle DEM = 90^{\circ}$ $\Delta ABC \leftrightarrow \Delta DEM$ $\overline{BC} \cong \overline{EM}$	(Supplementary angles) (Given) {from (i) and (ii)} (construction) (each ∠ equal to 90°)
	∠ABC≅∠DEM AB≅DE	(given)
∴ And	$\triangle ABC \cong \triangle DEM$ $\angle C \cong \angle M$ $\overline{CA} \cong \overline{MD}$	S.A.S. postulate (Corresponding angles of congruent triangles)
But	CA≅FD	(Concesponding sides of congruent triangles) (given)
∴ In	MD≅FD ΔDMF ∠F≅∠M	Each is congruent to CA FD≅MD (Proved)
Eut In 3	$\angle C \cong \angle M$ $\angle C \cong \angle F$ $\triangle ABC \leftrightarrow \triangle DEF$	(proved) (each is congruent to ∠M)
	$\overline{AB} \cong \overline{DE}$ $\angle ABC \cong \angle DEF$ $\angle C \cong \angle F$ e $\triangle ABC \cong \triangle DEF$	(given) (given) (proved) (S.A.A ≅ S.A.A)

Example

If perpendiculars from two vertices of a triangle to the opposite sides are congruent, then the triangle is isosceles.

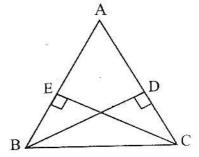
Given

In $\triangle ABC$, $\overline{BD} \perp \overline{AC}$, $\overline{CE} \perp \overline{AB}$

Such that $\overline{BD} \cong \overline{CE}$

To Prove

 $\overline{AB} \cong \overline{AC}$



Statements	Reasons
In $\triangle BCD \leftrightarrow \triangle CBE$ $\angle BDC \cong \angle BEC$	BD⊥AC,CE⊥AB(given)
BC≅BC	⇒ each angle = 90° Common hypotenuse
BD≅CE	Given
$\Delta BCD \cong \Delta CBE$ ∠BCD ≅ ∠CBE Thus ∠BCA ≅ ∠CBA	H.S. \cong H.S. Corresponding angles of $\cong \Delta s$.
Hence $\overline{AB} \cong \overline{AC}$	In ΔABC, ∠BCA ≅ ∠CBA

Exercise 10.4

In $\triangle PAB$ of figure, $\overrightarrow{PQ} \perp \overrightarrow{AB}$ and $\overrightarrow{PA} \cong \overrightarrow{PB}$. prove that $\overline{AQ} \cong \overline{BQ}$ and $\angle APQ \cong \angle BPQ$.

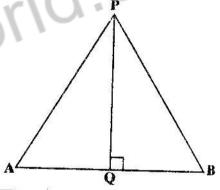
Crivere

In $\triangle PAB$, $\overrightarrow{PQ} \perp \overrightarrow{AB}$ and $\overrightarrow{PA} \cong \overrightarrow{PB}$

To Prove

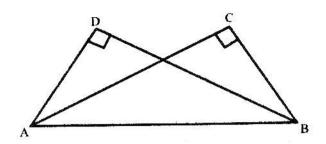
 $\overline{AQ} \cong \overline{BQ}$ and $\angle APQ \cong \angle BPQ$

Proof



	Statements	Reasons
In	$ \Delta APQ \leftrightarrow \Delta BPQ \overline{PA} \cong \overline{PB} \overline{PQ} \cong \overline{PQ} $	Given
:.	$\Delta PAQ \cong \Delta PBQ$	Common
••	$A\overline{Q} \cong \overline{BQ}$ $\angle APQ \cong \angle BPQ$	H.S ≅ H.S Corresponding sides of congruent triangles Corresponding angles of the congruent triangles.

In the figure, $m\angle C = m\angle D = 90^{\circ}$ and $\overline{BC} \cong \overline{AD}$. Prove that $\overline{AC} \cong \overline{BD}$ 2. and $\angle BAC \cong \angle ABD$.



Caven

$$\frac{m\angle C = m\angle D = 90^{\circ}}{BC \cong \overline{AD}}$$

To Prove

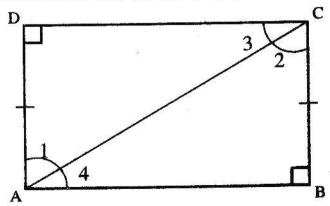
AC≅BD

∠BAC ≅ ∠ABD

Proof

	Statements	Reasons
In	$\triangle ABC \leftrightarrow \triangle ABD$ $m \angle C \equiv m \angle D$ $BC \cong \overline{AD}$ $\overline{AB} \cong \overline{AB}$ $\triangle ABC \cong \triangle ABD$	Each of 90° Given Common H.S ≅ H.S
)	AC≅BD ∠BAC≅∠ABD	Corresponding sides of congruent triangles Corresponding angles of the congruent triangles

3. In the figure, $m\angle B = m\angle D = 90^{\circ}$ and $\overline{AD} \cong \overline{BC}$. Prove that ABCD is a rectangle.



 $m \angle B = m \angle D = 90^{\circ}, \overline{AD} \cong \overline{BC}$

Proof

ABCD is a rectangle

	Statements	Reasons
In	$\triangle ABC \leftrightarrow \triangle ADC$	
	$ \underline{m} \angle B \cong m \angle D $	Each of 90°
	$\overline{AD} \cong \overline{BC}$	Given
	$\overline{AC} \cong \overline{AC}$	Common
	$\triangle ABC \cong \triangle ADC$	H.S ≅ H.S
	$\overline{AB} \cong \overline{DC}$	
	$\angle 1 \cong \angle 2$ (i)	
	$\angle 4 \cong \angle 3$ (ii)	1 (())
	$\angle 1 + \angle 4 = \angle 2 + m\angle 3$	120
	$\angle A = \angle C = 90^{\circ}$	z larlu.
	ABCD is a rectangle	By (i) and (ii)

- 4. Which of the following are true and which are false?
- (i) A ray has two end points.
- (ii) In a triangle, there can be only one right angle.
- (iii) Three points are said to be collinear if they lie on same line.
- (iv) Two parallel lines intersect at a point.
- (v) Two lines can intersect only in one point.
- (vi) A triangle of congruent sides has non-congruent angles.

Answers

- (i) False
- (ii) True
- (iii) True

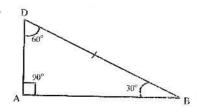
- (iv) False
- (v) True
- (vi) False

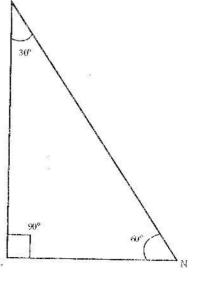
5. If $\triangle ABC \cong \triangle LMN$, then

- (i) m∠M ≅
- (ii) m∠N ≅
- (iii) m∠A ≅

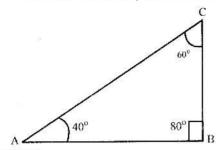
Answers

- (i) $m \angle M \cong m \angle B$
- (ii) $m \angle N \cong m \angle C$
- (iii) $m\angle A \cong m\angle L$





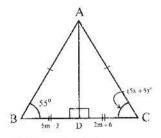
6. If $\triangle ABC \cong \triangle LMN$, then find the unknown x.



Answers

$$x = 60^{\circ}$$

7. Find the value of unknowns for the given congruent triangles.



 $\triangle ABD \cong \triangle ACD$

$$\overline{\mathrm{BD}} \cong \overline{\mathrm{DC}}$$

5m - 3 = 2m + 6
5m - 2m = 3 + 6
3m = 9
m =
$$\frac{9}{3}$$
 = 3

Also

Angles opposite to congruent sides are congruent

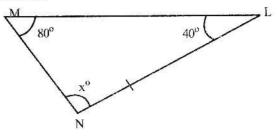
$$5x + 5 = 55$$

$$5x = 55 - 5$$

$$5x = 50$$

$$x = \frac{50}{5}$$

$$x = 10$$



8. If $\triangle PQR \cong \triangle ABC$

, then find the unknowns.

 $\Delta PQR \cong \Delta ABC$

$$\overline{PQ} \cong \overline{AB}$$

$$x = 3$$

$$\overline{BC} \cong \overline{QR}$$

$$\Rightarrow$$
 z = 4 cm

$$v - 1 = 5$$

$$y = 5 + 1$$

$$y = 6cm$$

$$\therefore$$
 x= 3cm, y = 6cm, z = 4cm

